

Estimating Parallel Efficiency

Parallel Efficiency

Goal: linear speedup

$$T(p) = \frac{T(1)}{p}$$

Reality: performance is lost

$$T(p) = \frac{T(1)}{e(p)p}$$

Efficiency $e(p) < 1$ reduces effective number of CPN

Why?

No general answer, too many factors

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Negative Factors

Simulation

- high number of sub-time-steps
- long boundaries
- slow data handling

Parallel Architecture

- load imbalances
- non-scalable control mechanisms

Communication

- slow encoding / decoding
- low bandwidth / high latency

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Assumptions for Traffic Simulation

Simulation Data Topology

- homogeneous street network,
- only local data dependencies,

Parallelization Technique

- domain decomposition

Simulation Control

- time-step driven system
- ignore statistics
- ignore control messages

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Boundary Communication

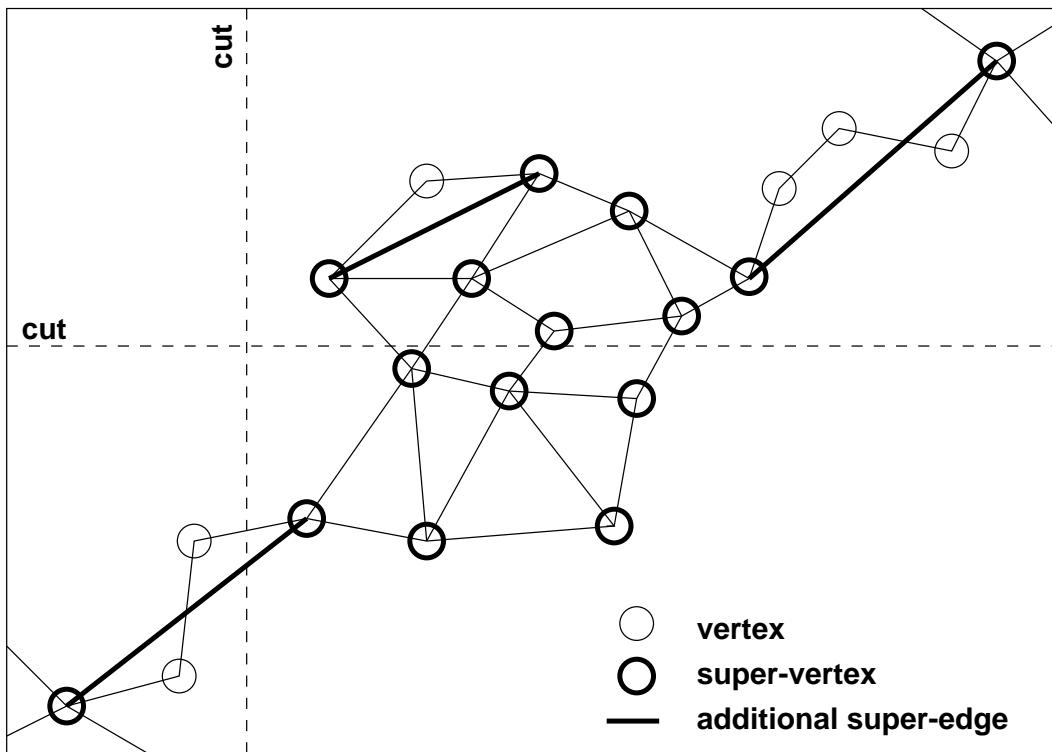
Most communication
is generated by
exchange of boundaries
on a
per sub-time-step
basis.

Two questions:

- How many boundaries are there?
- How long does it take to process the boundaries required in one time-step?

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How many boundaries?

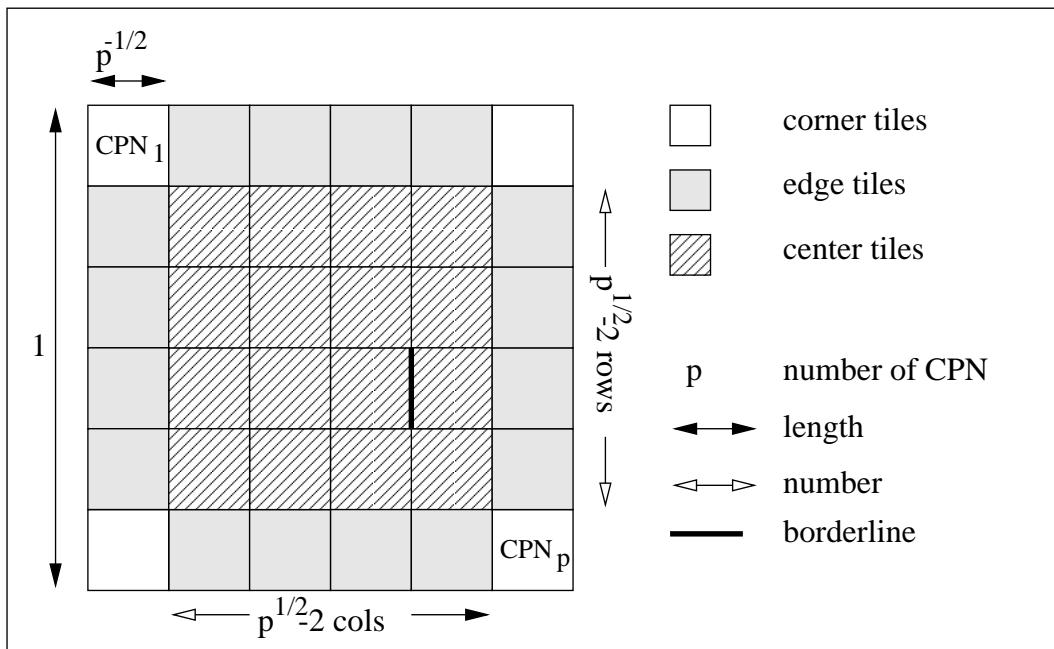


Assumption: All vertices with degree 2
have been replaced
 $\Rightarrow N$ super-vertices and E super-edges

What is the probability of
cutting a super-edge?

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Map Decomposition I



Number of Boundaries $B(p)$

$$\begin{aligned} B(p) = & \quad \varrho_E \quad (\text{edge density}) \\ & \times N(p) \quad (\text{number of borders}) \\ & \times l_b(p) \quad (\text{border length}) \end{aligned}$$

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Map Decomposition II

Edge Density

$$\varrho_E(p) = \sqrt{N} \frac{\deg(G)}{2} = \sqrt{N} \frac{2E}{2N} = \frac{E}{\sqrt{N}}$$

Number of Borders (Neighbours)

$$N(p) = 8 + 12(\sqrt{p} - 2) + 4(\sqrt{p} - 2)^2$$

Border Length

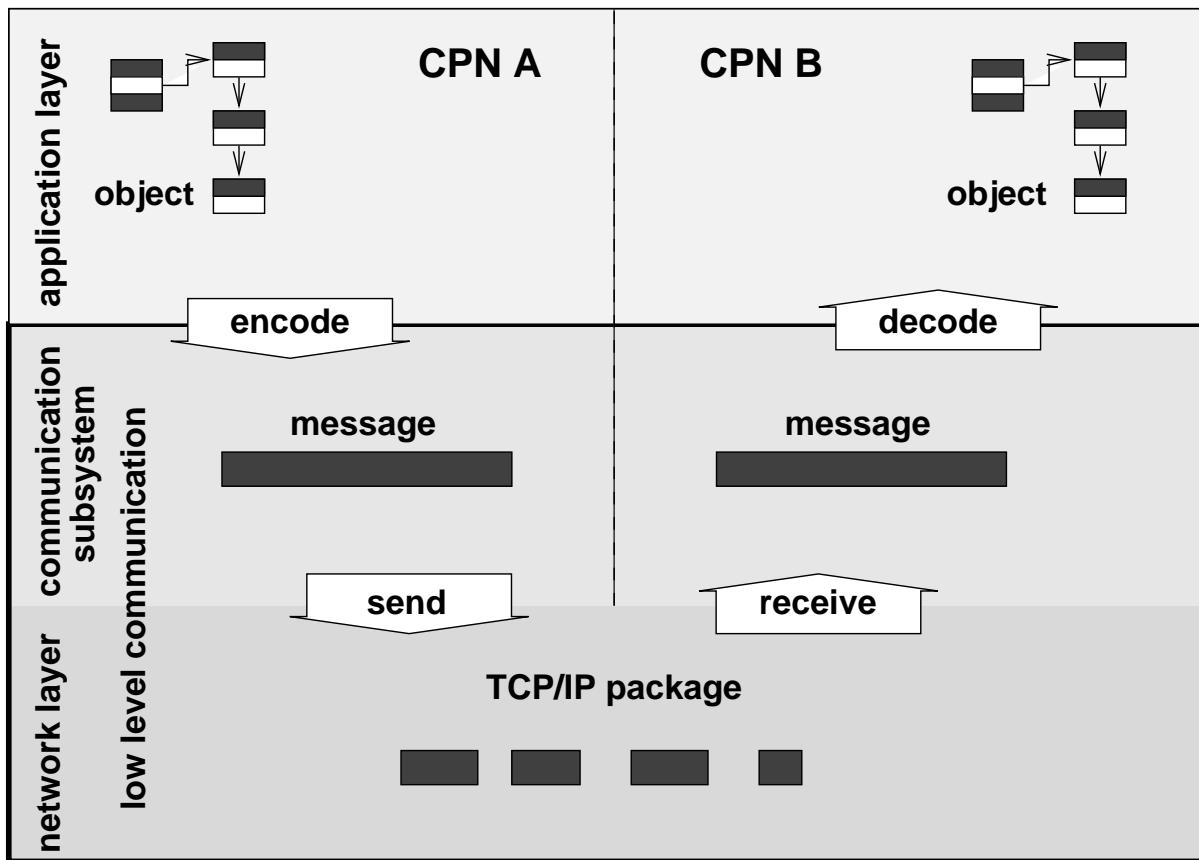
$$l_b(p) = \frac{1}{\sqrt{p}}$$

$$B(p) = O(\sqrt{p})$$

Number of boundaries **does not scale!**

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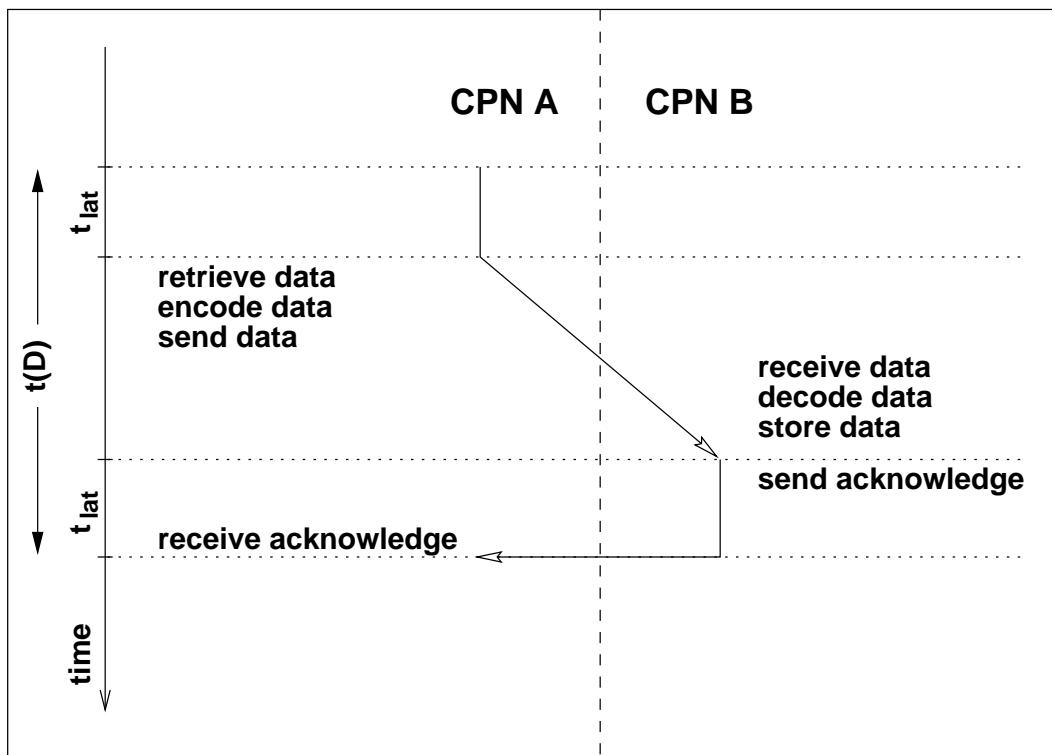
Tracing a Boundary



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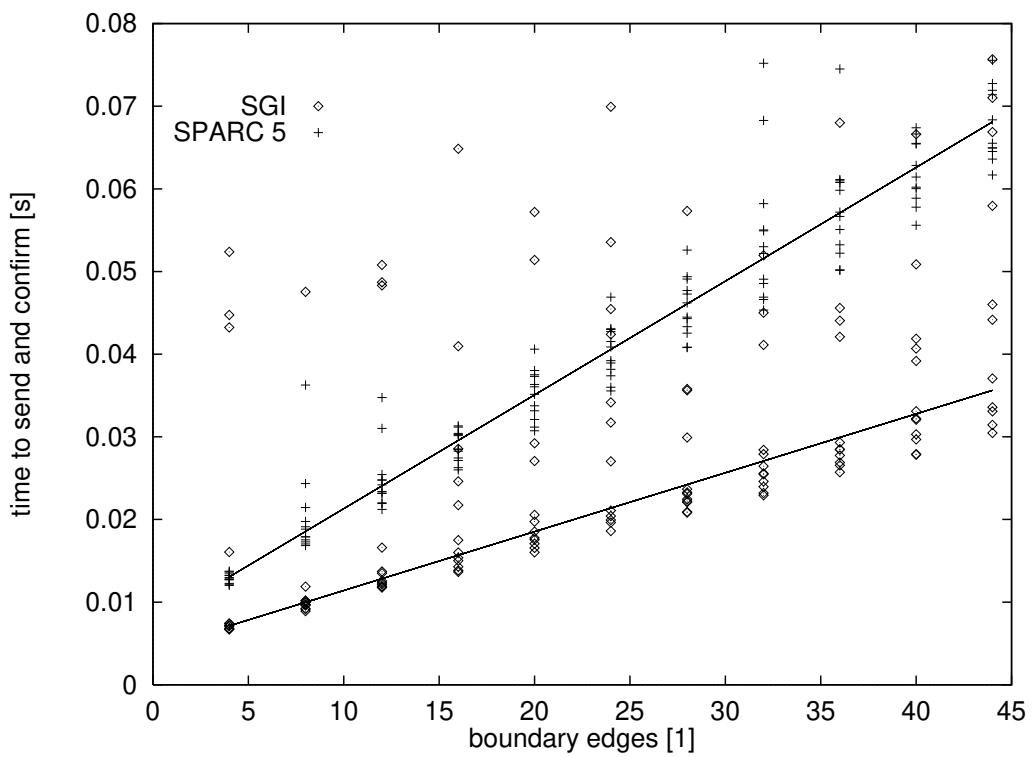
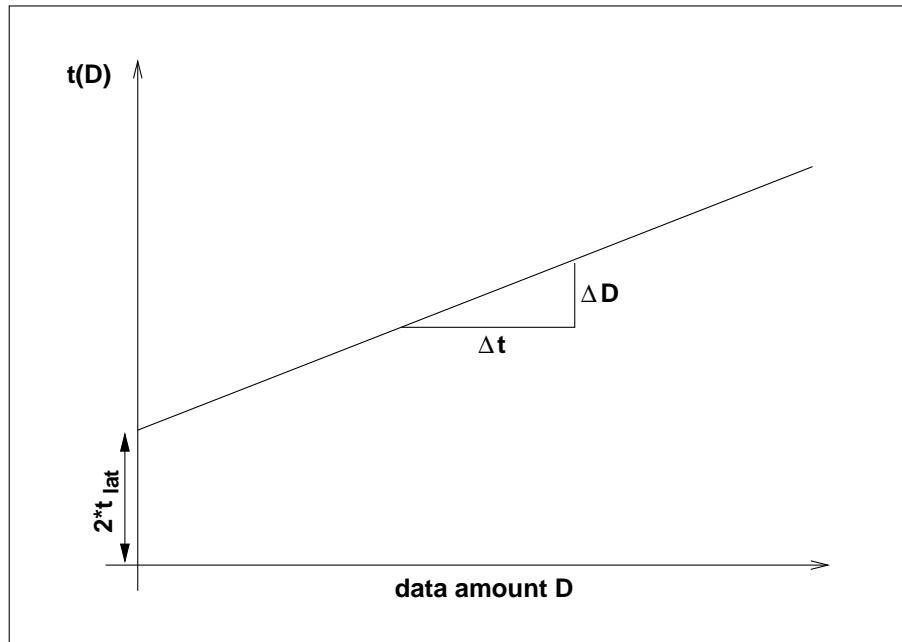
Measuring Application-level Latency and Bandwidth

Measure the time $t(D)$ for
retrieving, encoding, sending,
receiving, decoding, and storing
amount D data
plus an additional acknowledge .



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Measurements



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Network Saturation I

Assumptions for application-level communication only hold, if communication network is not loaded otherwise!

Multiple CPN have to share the same network bandwidth.

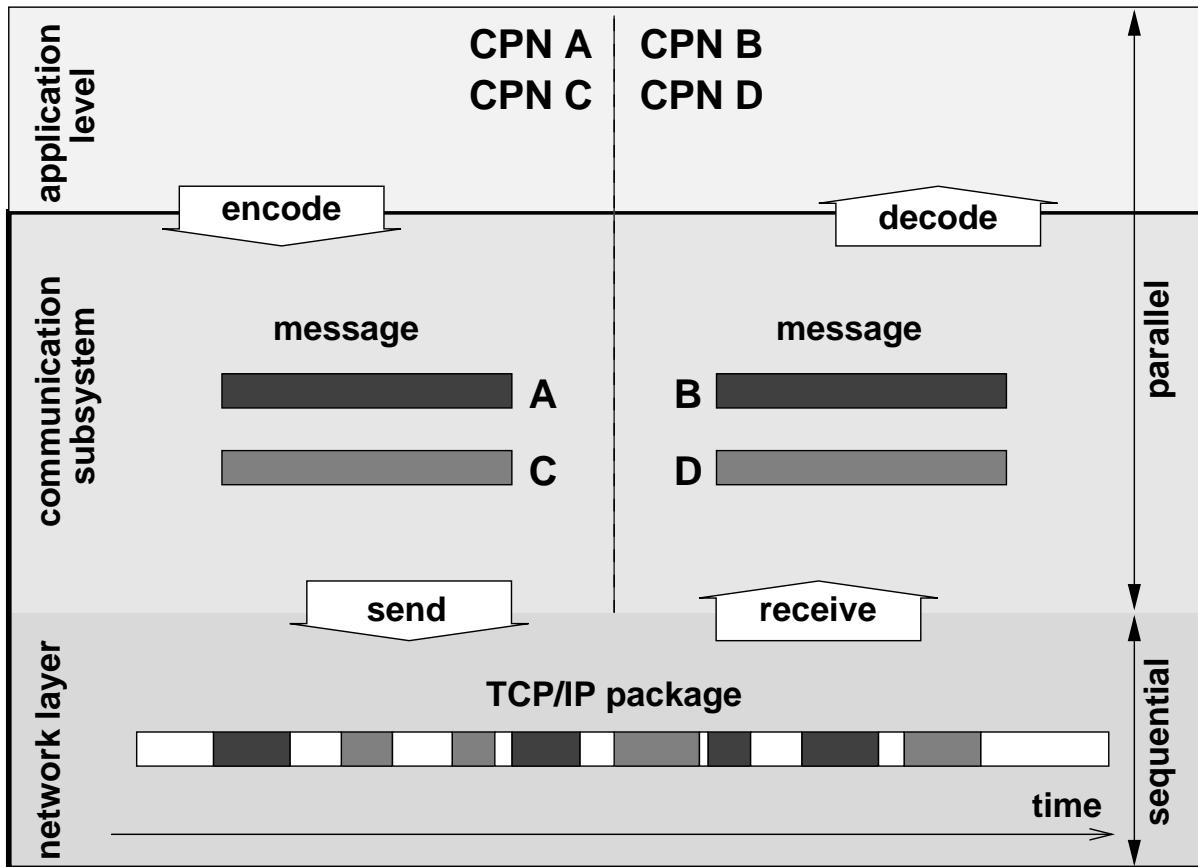


Above a certain number of CPN, communication performance may be dominated by low-level communication.

Depends on communication network topology!

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Network Saturation II

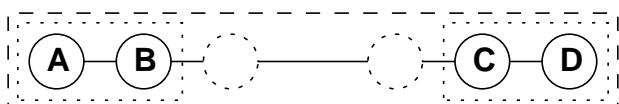


Low-level communication scales
until
all gaps are filled!

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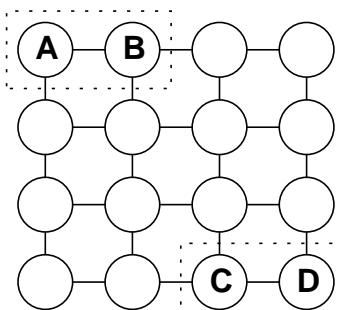
Communication Network Topologies

bus topology



locally sequential
globally sequential

2-D grid topology



Bus-Topology

- no difference between local and non-local communication
- all communication is sequential

2D-Grid-Topology

- local communication is sequential,
- but globally parallel

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Traffic Simulation with 2D-Grid

Bus-Topology:

All boundaries between CPN have to be transferred sequentially

⇒

$$B_{seq}(p) = B(p) = O(\sqrt{p})$$

2D-Grid-Topology:

Only local boundaries have to be transferred sequentially

⇒

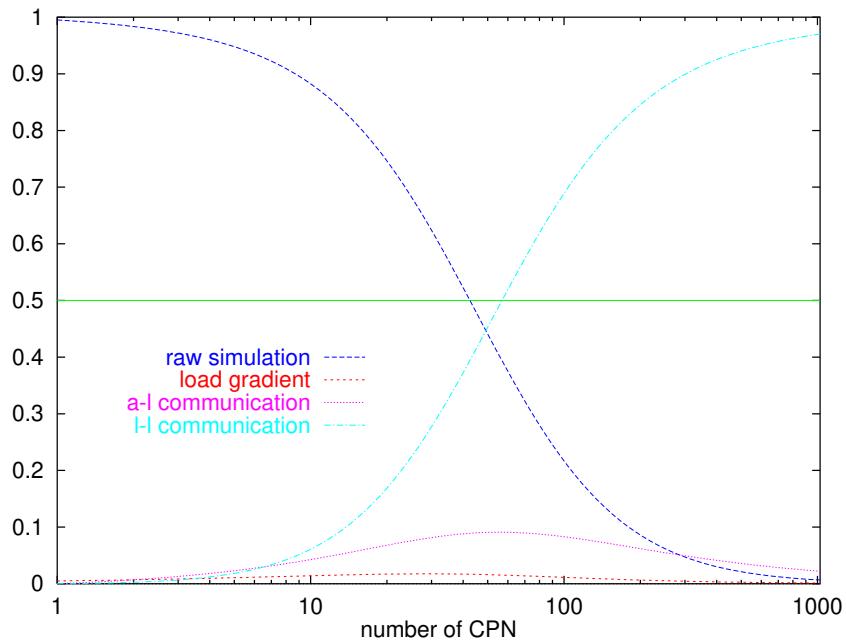
$$B_{seq}(p) \sim \frac{B(p)}{p} = O(1 + 1/\sqrt{p})$$

Boundary communication scales perfectly!

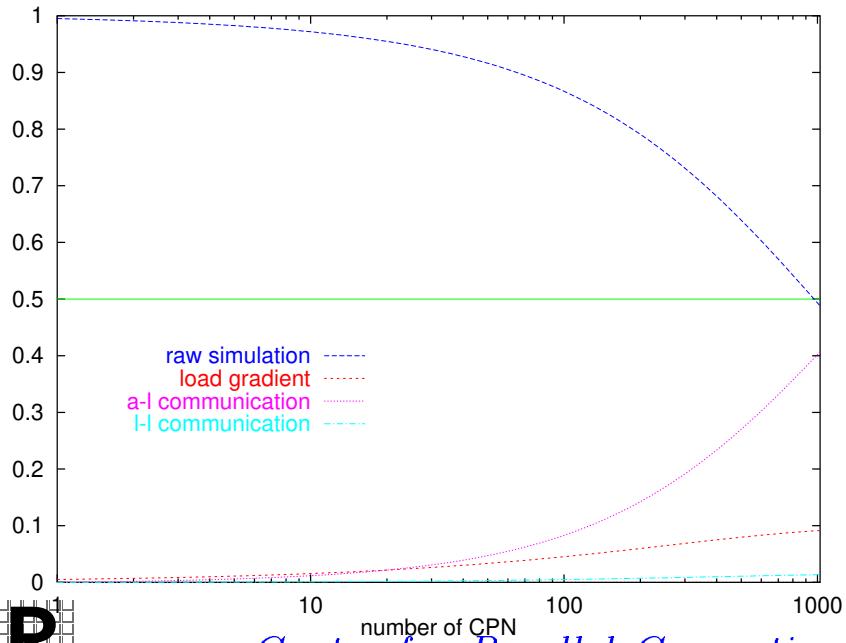
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Efficiency

Sparc Cluster

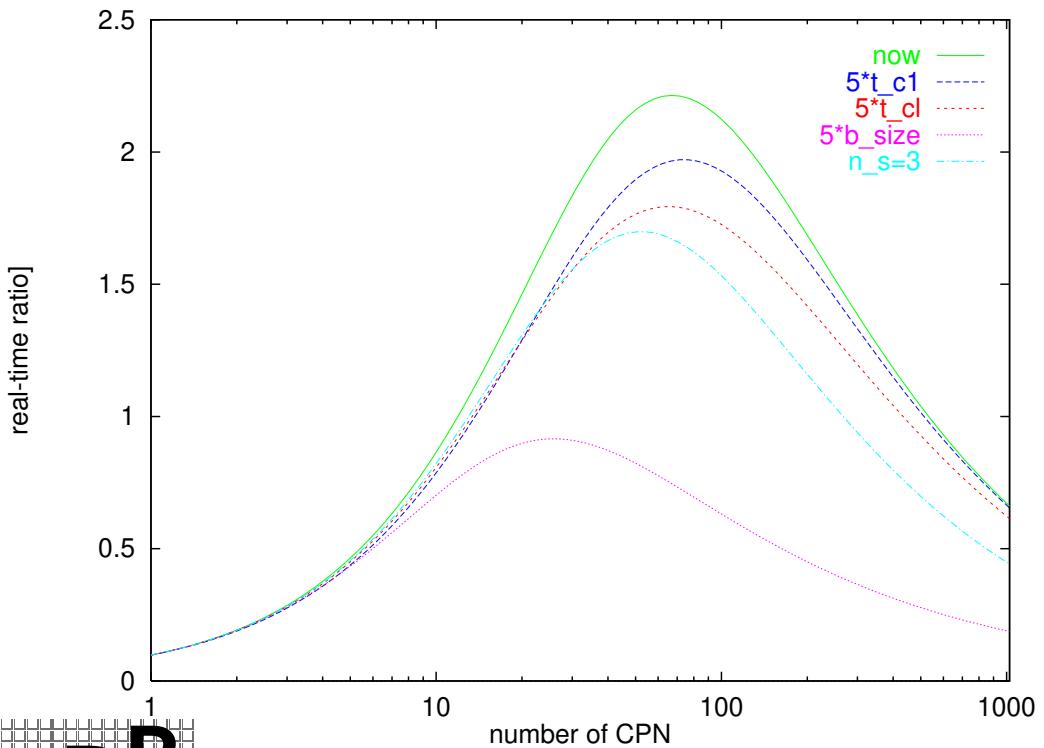
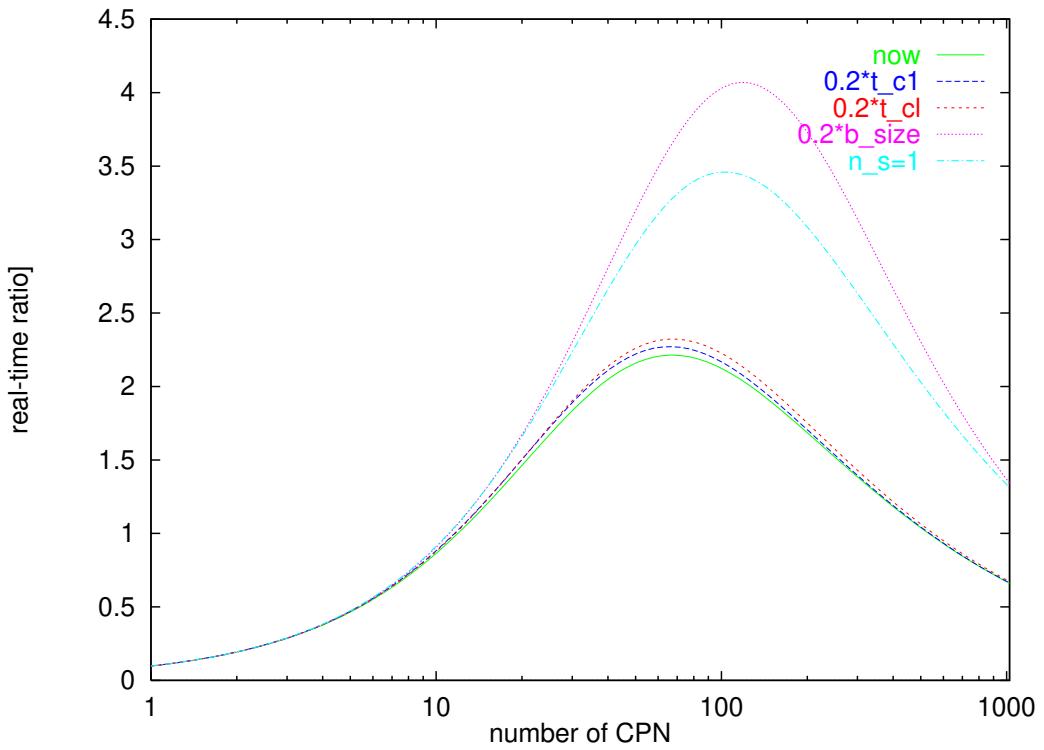


Paragon



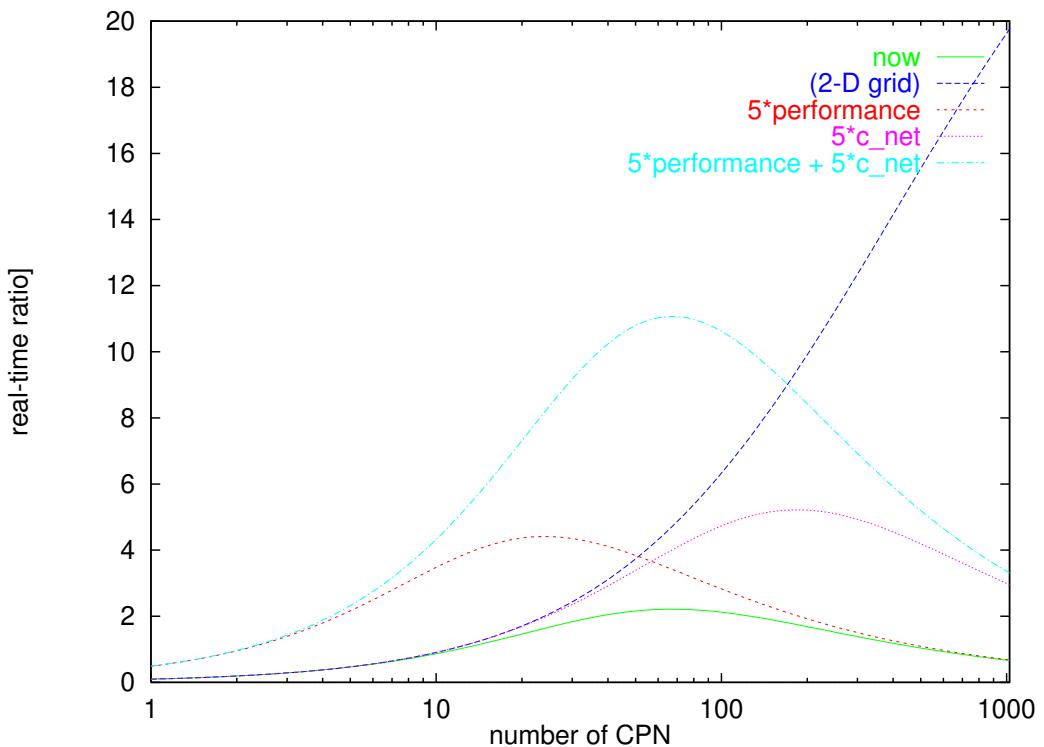
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Software Modifications



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Hardware Modifications



Guidelines I

- Keep boundaries as short as possible
 - ⇒ reduce low-level communication saturation
 - Keep boundary handling simple
 - sort data items according to data types
 - use arrays instead of lists (at lowest level)
 - implement short “delivery paths” for messages
- ⇒ reduce application-level communication time

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Guidelines II

- “anticipate” what boundary information is required instead of waiting for requests
⇒ reduce number of sub-time-steps



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